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DEVELOPMENT OF AN OPEN ROTOR CYCLE MODEL IN NPSS USING A MULTI-DESIGN POINT APPROACH

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ABSTRACT

NASA's Environmentally Responsible Aviation Project and Subsonic Fixed Wing Project are focused on developing concepts and technologies which may enable dramatic reductions to the environmental impact of future generation subsonic aircraft [1][2]. The open rotor concept (also referred to as the Unducted Fan or advanced turboprop) may allow the achievement of this objective by reducing engine emissions and fuel consumption. To evaluate its potential impact, an open rotor cycle modeling capability is needed. This paper presents the initial development of an open rotor cycle model in the Numerical Propulsion System Simulation (NPSS) computer program which can then be used to evaluate the potential benefit of this engine.

The development of this open rotor model necessitated addressing two modeling needs within NPSS. First, a method for evaluating the performance of counter-rotating propellers was needed. Therefore, a new counter-rotating propeller NPSS component was created. This component uses propeller performance maps developed from historic counter-rotating propeller experiments to determine the thrust delivered and power required. Second, several methods for modeling a counter-rotating power turbine within NPSS were explored. These techniques used several combinations of turbine components within NPSS to provide the necessary power to the propellers. Ultimately, a single turbine component with a conventional turbine map was selected.

Using these modeling enhancements, an open rotor cycle model was developed in NPSS using a multi-design point approach. The multi-design point (MDP) approach improves the engine cycle analysis process by making it easier to properly size the engine to meet a variety of thrust targets throughout the flight envelope. A number of design points are considered including an aerodynamic design point, sea-level static, takeoff and top of climb. The development of this MDP model was also enabled by the selection of a simple power management scheme which schedules propeller blade angles

with the freestream Mach number. Finally, sample open rotor performance results and areas for further model improvements are presented.

INTRODUCTION

Passenger travel by commercial aviation is expected to grow at a steady pace over the next 10-15 years [3][4][5]. This expected increase in the number of passengers will place significant strain on the current air transportation system. In addition to creating more congestion and delays, the increase in air travel will amplify aviation's impact on the environment [4][6][7]. Therefore, several of NASA's primary goals for the future are the significant reduction of aircraft fuel burn, community noise, emissions of nitrogen oxides (NO_x) and field length for the next generation of commercial single aisle aircraft [1][2]. These aggressive goals are used to develop technology roadmaps and guide technology research efforts across a number of research disciplines.

A technology area of particular interest to NASA and the commercial aviation industry is that of advanced engine concepts [8]. One specific concept in this research area that is receiving considerable attention is the open rotor as it has the potential to dramatically reduce aircraft fuel consumption. The open rotor concept achieves these reductions by using a large, counter-rotating advanced propeller as shown in Figure 1. The advanced counter-rotating propeller allows for many of the fuel efficiency benefits of a traditional turboprop to be achieved without the sacrifice of maximum aircraft speed typically required. The open rotor engine concept was originally developed during the 1980's under the NASA's Advanced Turboprop Project [9], and demonstrated significant fuel burn reductions. However, due to reduced fuel prices and several technical challenges facing open rotor implementation, the concept was not developed further.

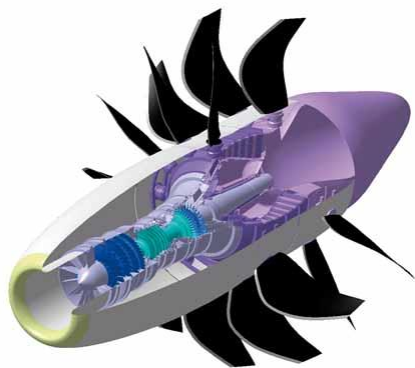


Figure 1. Cutaway of a Notional Open Rotor Concept [10].

While the open rotor engine developed during the Advanced Turboprop Project demonstrated significant reductions in fuel consumption, the lack of development over the last two decades has allowed conventional turbofans to close the performance gap [9][11]. However, many of the technological improvements which have been made to turbofans can also be applied the open rotor, thereby further improving its performance. In addition, advances in computing and design are enabling the creation of more advanced counter-rotating propeller blades. With these improvements to both conventional gas turbine components and counter-rotating propellers, there is a need to evaluate the potential improvements available in open rotor engines. The development of a new analytical cycle model is critical to the evaluation of conceptual open rotor aircraft designs such as those shown in Figure 2.

This paper summarizes the development of an open rotor engine cycle model with the NPSS computer program. NPSS is a variable-fidelity, object-oriented, engine cycle analysis tool developed jointly by NASA and U.S. industry [12][13]. It is currently the accepted, state-of-the-art software for airbreathing engine cycle performance analysis for U.S. aerospace industry, academia, and NASA. In the next few sections, the following topics related to the open rotor cycle model development will be addressed:

- Selection of an open rotor engine architecture and implementation in NPSS
- NPSS model enhancements for counter-rotating propeller performance prediction
- Potential solutions for estimating counter-rotating turbine performance in NPSS
- Implementation of a multi-design point formulation to improve process for creating candidate engine models
- Determination of a power management strategy allowing for performance estimation throughout the flight envelope
- Presentation of sample engine performance results
- Areas for further model improvements



Figure 2. Notional Open Rotor Airplane Concepts [14][15].

NOMENCLATURE

A	Propeller Annulus Area
ADP	Aerodynamic Design Point
Alt	Altitude
β	Front Blade angle
C_p	Net Power Coefficient, $P / \rho n^3 D^5$
C_T	Thrust Coefficient, $F_g / \rho n^2 D^4$
D	Diameter
ENET	Net Propeller Efficiency, $J C_T / C_p$
F_g	Propeller Gross Thrust
FAR	Fuel to Air Ratio
Δh	Specific Enthalpy Change
HP	High Pressure
HPC	High Pressure Compressor
HPT	High Pressure Turbine
ISA	International Standard Atmosphere
J (or J1C)	Front Rotor Advance Ratio, V / nD
LP	Low Pressure
LPC	Low Pressure Compressor
LPT	Low Pressure Turbine
M	Mach Number
MDP	Multi-Design Point
N, n	Rotation Speed
NPSS	Numerical Propulsion System Simulation
PQA	Modified Power Coefficient, $P / \rho n^3 D^3 A$
PQAJ3	Modified Power Coefficient divided by Advance Ratio cubed
PT	Power Turbine
SLS	Sea-Level Static
T	Temperature
T4	Combustor Exit Temperature

TO	Takeoff
TOC	Top of Climb
TSFC	Thrust Specific Fuel Consumption
TQA	Modified Thrust Coefficient, $F_g / \rho n^2 D^2 A$
UDF	Unducted Fan

Figure 4. Open Rotor Block Diagram.

COUNTER-ROTATING PROPELLER MODELING

The performance data reported for the F7/A7 was from wind tunnel tests and was presented as shown in Figure 5. In the top plot, the modified total power coefficient (PQA) is shown as a function of the front propeller advance ratio ($J1C$) and propeller blade angles (each line represents a single combination of front and aft blade angles). In the bottom plot, the net efficiency of the counter-rotating propellers is shown as a function of the power coefficient divided by advance ratio, cubed (PQAJ3) and propeller blade angles. Plots such as these were given as several different Mach numbers to describe the semi-installed performance (the effects of the upstream nacelle are captured, but not an upstream pylon) at several points throughout the flight envelope [17]. In addition, limited data were provided describing the distribution of torque between the blade rows at several flight conditions and blade angles.

In order to improve the estimation of the thrust coefficient, power coefficient and efficiency at extrapolated points, the

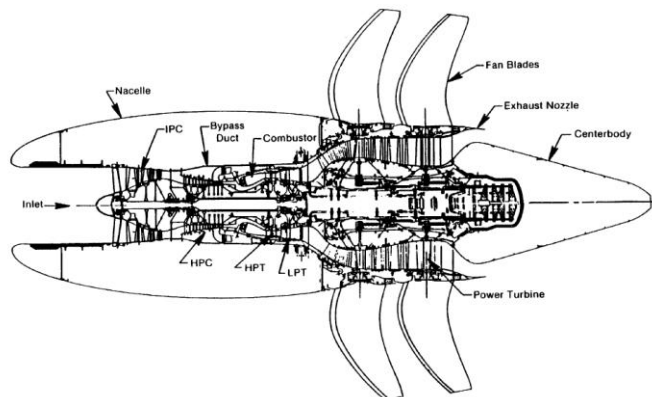


Figure 3. GE36 UDF Cross Section [16].

With this architecture selected, an engine model could be developed in NPSS. The engine was decomposed into a series of components as shown in Figure 4. Most of the blocks shown in Figure 4 are blue as NPSS already contains analysis capabilities for these components. The green blocks, however, identify two unique engine components which were not readily available in NPSS. As a result, solutions needed to be identified for how to model the counter-rotating propeller and counter-rotating turbine within NPSS. The next two sections will describe the steps taken to estimate the performance of the counter-rotating propellers and turbine using available performance data.

tables were replaced with response surface equations (multi-variable regression equations) which relate performance to Mach number, advance ratio and blade angle. These equations better capture the trends in the data in comparison to interpolating and extrapolating based on tables. Therefore, a set of response surface equations fit to the F7/A7 performance data were developed for use in this model and are provided in Annex A.

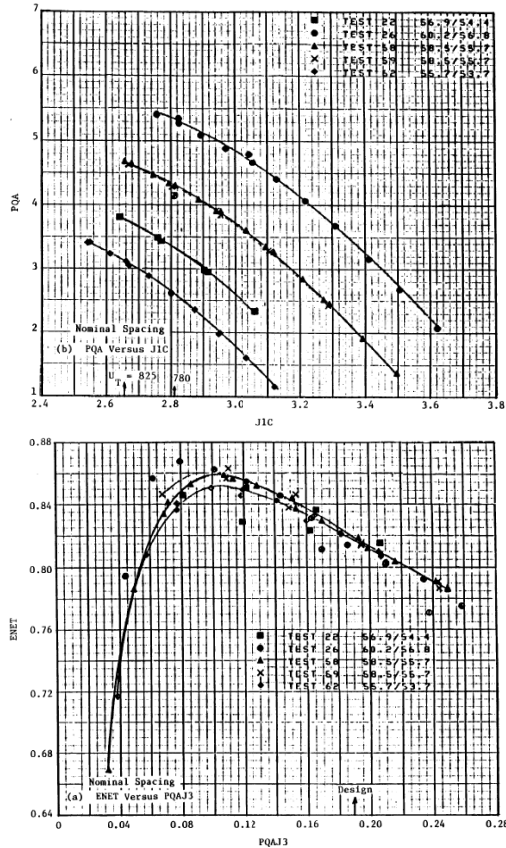


Figure 5. F7/A7 Propeller Performance Data at Mach 0.72 [17].

With the propeller performance data captured in the maps, a counter-rotating propeller element was written for NPSS which computes the performance of counter-rotating propellers as engine components. The NPSS counter-rotating propeller element has a fluid input port and fluid output port along with a shaft port for each blade row. When the engine is being evaluated in design mode, the design blade angle and the propeller diameter are determined based on the specified total power requirements, rotation speed and disk loading. In off-design mode, the propeller power required and thrust produced are determined from input flight conditions, rotation speed and blade angles.

COUNTER-ROTATING TURBINE MODELING

One of the challenges associated with modeling this open rotor configuration is the counter-rotating turbine which drives the propellers. A notional schematic of the counter-rotating turbine and propellers as used in the GE36 UDF is shown in Figure 6. In this configuration, the only static blade rows are the inlet and exit guide vanes. The remaining blade rows in the power turbine all rotate, with odd and even numbered rows rotating in opposite directions. This can be seen in Figure 6 as the solid blade rows will rotate in one direction, while the hatched blade rows will spin in the opposite direction. This configuration is unique resulting in little historic data and analytical analysis capabilities existing for this type of turbine. A partial performance map for the GE36 counter-rotating power turbine was found as shown in Figure 7 giving some insight into the performance. However, this overall power turbine map does not include information on turbine pressure ratio and mass flow limiting its utility. An additional limitation of the map is that it is applicable only when there are equal rotation speeds for the two propulsor shafts. This lack of data and analysis capabilities make it difficult to model the counter-rotating turbine in NPSS, requiring exploration of several counter-rotating turbine performance estimation techniques.

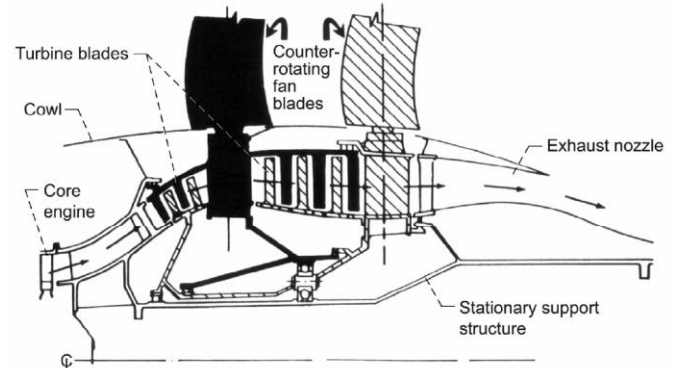


Figure 6. Schematic of GE36 Power Turbine [18].

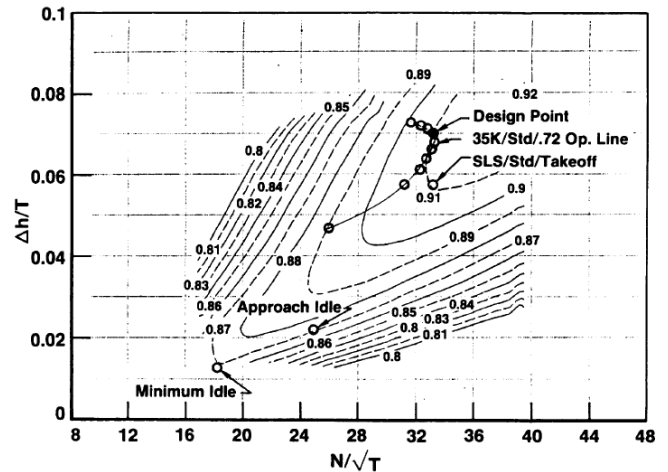


Figure 7. GE36 Overall Power Turbine Performance Map [19].

The first technique examined focused on trying to match what would be physically occurring in the counter-rotating turbine. Specifically, it was assumed that the work being extracted in an alternating fashion for the two propulsor shafts was an important characteristic to capture. Therefore, a blade row by blade row model was implemented in NPSS by placing 12 turbine elements (the same as the number of blade rows in the GE36) in series and linking their flow ports. These twelve turbines were then linked alternately to two shaft elements. This turbine setup required several additional parameters to implement properly. During design, the work distribution across the 12 stages needed to be specified and was set to values similar to those described in the GE36 Design Report [19]. Furthermore, the performance of each blade row at all operating conditions needed to be estimated and was done by applying a performance map for a traditional, single stage turbine to each blade row. The performance maps of each blade row were then scaled such that the desired total power turbine adiabatic efficiency was achieved providing similar performance to the GE36 power turbine [19].

The results of implementing this power turbine modeling method were mixed. In the region near the design turbine design point, the total turbine performance map generated by the blade row by blade row model provided efficiency contours of similar shape to those shown in Figure 7. However, at off-design cases farther away from the design point the quality of this modeling approach deteriorated as the model often would not converge or would converge on a physically infeasible solution. The most common observation was that the last blade row in the power turbine would act as a compressor, absorbing power and raising the pressure across the row. The precise cause of this numerical phenomenon has not been determined, but there are several possible factors that may be contributing. First, the performance maps used for each blade row did not capture changes to inflow swirl from the preceding stage. Therefore, changes to performance from variations in rotation speeds of both shafts were not captured. Second, the work extraction distribution across the stages which was specified at design may be incorrect, resulting in too little energy being available in the last stages of the turbine. Finally, the power split determined in the counter-rotating propeller map (which is based on sparse data) may be driving the solution to an unrealistic result. Due to these results, the blade row by blade row power turbine model was not pursued further, but may be considered again in the future.

Next, two simplified power turbine models were considered. First, the power turbine was modeled using two conventional turbine components in series. This modeling approach eliminates the single blade row map and work extraction issues of the blade row by blade row model while still allowing both propellers to be driven independently. However, the implementation of this method in NPSS still did not produce acceptable off-design performance. These results indicate that there is likely an interaction between the counter-rotating propeller and power turbine which is not correctly

addressed with both this method and the blade row by blade row turbine model.

Finally, a single, traditional, low pressure turbine NPSS element was used to drive the entire counter-rotating propeller system. This method assumes that only the total power passed between the power turbine and propellers is important (it does not take into account the power split between the rotors). The method also forces the rotation speed of the propellers to be equal. Therefore, the single NPSS component power turbine model was implemented in the NPSS open rotor model. This technique was also selected by Bellocq et al. in their study of open rotor performance modeling [20].

MULTIPLE-DESIGN POINT FORMULATION

Through the development of the counter-rotating propeller and turbine modeling capabilities in NPSS, a complete NPSS model of an open rotor turbine engine model was constructed following the block diagram of Figure 4. While this block diagram details the layout of components within the engine, it does not describe the process which will be used to size the engine to meet various performance requirements throughout the flight envelope. The traditional engine cycle design process uses a single design point (cruise or takeoff) to size the engine. The off-design performance is then evaluated to determine if thrust targets are met at other flight conditions. If thrust targets are not met at these other flight conditions, the engineer must manually change parameters at the design point until all the thrust targets are met. This process can be quite tedious, especially for unconventional engines such as the open rotor where the engineer has little intuition regarding the effect of changing design point variables.

In order to improve the process of sizing the open rotor engine to meet multiple thrust targets, the open rotor model is being implemented using a multiple-design point formulation. In this formulation, the NPSS model is constructed so that all critical flight conditions are evaluated simultaneously to ensure all thrust targets and other design requirements are met. Therefore, each designed engine is guaranteed to meet the performance requirements specified by the designer. This technique was proposed and evaluated in academia for NPSS by Schutte [21] and is capable of handling a larger number of design points. The rest of this section will describe some of the details regarding the implementation of the open rotor in an MDP formulation.

First, the design points and their associated thrust targets need to be identified. For a typical engine, several design points including top-of-climb, takeoff and sea-level static are often considered. Table 1 lists several example design points which were considered in the development of this open rotor model. The aerodynamic design point (ADP) refers to a throttled back operating point representative of a cruise condition where the turbomachinery components would be designed for best performance. For example, this would be the flight condition and throttle setting at which the propellers were designed.

Table 1. Design Points for MDP Formulation.

Design Point	Mach	Alt (ft)	ΔT (°F) (from ISA)	Net Thrust (lbf)
ADP	0.72	35,000	+0	n/a
TOC	0.72	35,000	+0	4,600
TO, Hot Day	0.25	0	+27	17,500
SLS, Hot Day	0.00	0	+27	25,000

From the list provided in Table 1, two design points were selected for the current study: top-of-climb and hot day takeoff. These two points were selected as they were the two primary thrust targets for this engine. There was not enough information available regarding the throttled back cruise condition to define an aerodynamic design point; therefore, the TOC point was used as the ADP of the turbomachinery components. Using these two design points, the MDP model was constructed by adding the parameters below to the NPSS solver. Of these five independent/dependent pairs, the first three allow the sizing of the engine for matching the thrust targets at both TOC and TO. The last two independents and dependents size the propeller in relation to the gas generator at TOC and ensure that the F7/A7 design characteristics are matched.

Table 2. NPSS Solver Variables for MDP Formulation.

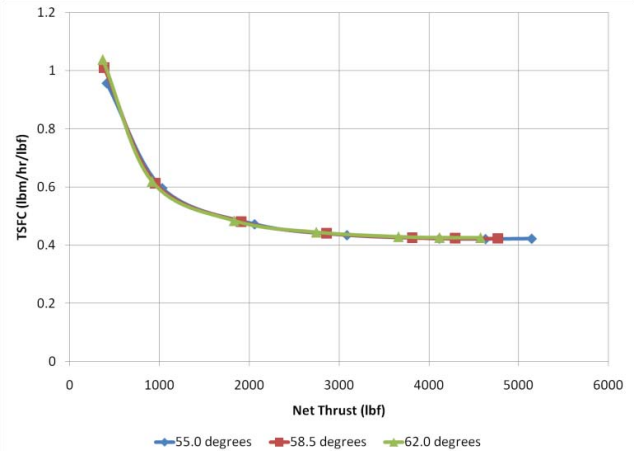
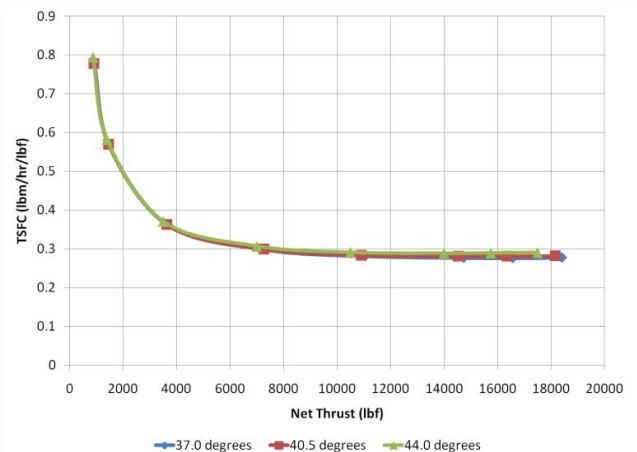
NPSS Independent	NPSS Dependent
TOC Core Mass Flow	TO Net Thrust
TOC FAR	TOC Net Thrust
TO FAR	TO T4 Max
TOC Propeller Power	TOC Nozzle Pressure Ratio
TOC Propulsor Speed	TOC Propeller Tip Speed

Within the NPSS, the solver is varying these independent parameters in order to achieve specific values of the dependent variables at the appropriate flight conditions (in addition to other independents and dependents automatically added to the solver). Therefore, target values for each dependent must be specified. For the first three dependents, the target values are determined by the thrust requirements and technology assumptions being used by the designer. The propeller tip speed target is determined from the propeller design process. For the F7/A7, the design front propeller tangential tip speed was 780 feet per second. Finally, the core nozzle pressure ratio must be specified as it determines the relative size of counter-rotating propellers and core engine. For this study a nozzle pressure ratio of 1.25 was selected at TOC. By selecting this value for nozzle pressure ratio, almost all the energy is being extracted from the core flow to drive the counter-rotating propellers. Therefore, almost all the thrust is being produced by the high efficiency propellers, lowering the engine TSFC. While this value for nozzle pressure ratio is low at the TOC design point, it allows enough margin so that the pressure ratio remains above unity throughout the flight envelope.

POWER MANAGEMENT STRATEGY

Another challenge in developing the open rotor MDP model was selecting a method for controlling the engine at each operating point in the flight envelope. The control of the open rotor engine differs from a traditional turbofan because both the propeller blade angle and combustor fuel flow can be varied. Therefore, a strategy for controlling both of these parameters throughout the flight envelope was required to allow for the proper sizing of engine in the MDP and estimation of performance in off-design operation.

In order to develop the proper power management strategy, several brief studies were conducted to determine relevant trends in the engine operation. Figure 8 below shows a powerhook for the engine at cruise with three different blade angles. The figure shows that for all three blade angles, the powerhooks are nearly identical for most of the operating range. The significant difference occurs at the maximum thrust setting for each blade angle. The maximum thrust for each blade angle differs as a result of other constraints on the engine operation such as the maximum combustor exit temperature, maximum LPC corrected speed and maximum propeller rotation speed. Similar trends are observed at takeoff conditions as shown in Figure 9.

**Figure 8. Mach 0.72, 35k ft Powerhooks.****Figure 9. Mach 0.25, Sea-Level Powerhooks.**

Using the results of these studies, a simple blade angle schedule was selected as shown by the green line in Figure 10. This characteristic was selected as it passes through the known F7/A7 design point and falls within the bounds of the reported experimental data at all Mach numbers. By selecting a single front propeller blade angle at each Mach number, a reasonable prediction of the conceptual open rotor performance can be obtained throughout the flight envelope. It is recognized that the schedule selected in Figure 10 will provide a conservative estimate of the maximum thrust available as seen in Figure 8 and Figure 9. Following the development of this schedule, additional data which covers a larger range of Mach numbers was found for the F4/A4 and F5/A5 open rotor blade sets. These blade sets were developed around the same time as the F7/A7 for a similar cruise Mach number, but had different blade geometry. [17]. While this data was not reported in the context of a power management strategy, the front blade angle of both blade sets follows a linear trend similar to that selected for the F7/A7, supporting the use of this schedule for preliminary performance evaluation. Future refinement of this schedule may allow for improved prediction of maximum thrust at each flight condition.

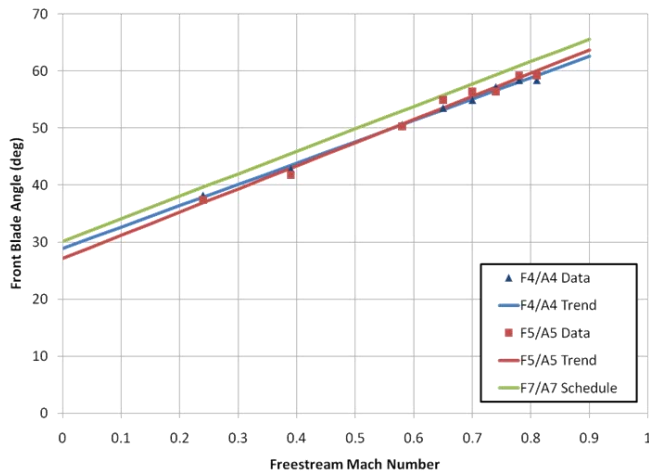


Figure 10. Front Propeller Blade Angle Schedule.

Several other options for developing a power management scheme have also been considered which would provide more complex control of blade angle and fuel flow. One option is to use an optimizer to select the blade angle resulting in the minimum TSFC at a given T_4 . The advantage of this technique is that it would allow for the proper blade angle at every point analyzed and the scheme would be rapidly adjustable to new designs. However, the inclusion of an optimizer in NPSS model substantially lengthens the execution time and often results in numerical stability problems. Other power management schemes are also being investigated based on more detailed studies of the operating characteristics of the engine. In this case, it may be possible to use the identified characteristics in conjunction with the NPSS solver to select the appropriate blade angle and fuel flow settings. The difficulty

observed with this method to date is the operating characteristics of the engine do not appear to be consistent throughout the flight envelope making it difficult to set up the proper NPSS solver variables.

SAMPLE PERFORMANCE RESULTS

The open rotor modeling enhancements described in the previous sections were used to construct a complete NPSS model of the gearless, pusher engine. The model uses the F7/A7 counter-rotating propeller driven by a single power turbine component. The MDP setup contains only TOC and TO points with the blade angle determined by the simple schedule presented above.

Using the developed model, a notional open rotor engine was created for evaluation. The results presented in this section are examples intended to demonstrate the capabilities of the model and results which can be produced. A summary of the open rotor engine cycle parameters used to generate the sample results is provided in Table 3. Values for core component design parameters were selected to represent advanced technology levels while power turbine and counter-rotating propellers parameters were selected to represent expected improvements over the GE36 Unducted Fan.

Table 3. Cycle Definition at TOC (* at TO).

Component	Parameter	Value
LPC	Pressure Ratio	2.4
	Adiabatic Efficiency (%)	87.6
HPC	Pressure Ratio	17.7
	Adiabatic Efficiency (%)	87.8
Burner	Exit Temperature ($^{\circ}$ R)*	3460
HPT	Adiabatic Efficiency (%)	92.1
LPT	Adiabatic Efficiency (%)	94.1
PT	Adiabatic Efficiency (%)	92.0
Counter-Rotating Propellers	Net Efficiency (%)	85.0
	Front Tip Speed (ft/s)	780
	Power Loading (shp/D ²)	55.5

Evaluating the open rotor NPSS model with these inputs produces the results given in Table 4. While this engine was not designed to exactly match the GE36, it is comparable in the overall size and thrust as shown in Table 5. The sample engine presented here has a slightly smaller propeller diameter and SLS thrust. However, it also demonstrates a lower TSFC due to the utilization of a modern gas generator. In addition, further improvements in the TSFC of the sample open rotor may be possible with further design and optimization.

Table 4. Open Rotor Cycle Results.

Parameter (units)	Value
Front Propeller Diameter (ft)	10.9
TOC Core Mass Flow (lbm/s)	19.6
TOC Net Thrust (lbf)	4600
TOC Propeller Thrust (lbf)	4410
TOC TSFC (lbm/hr/lbf)	0.394
TO Core Mass Flow (lbm/s)	43.8
TO Net Thrust (lbf)	17,500
TO Propeller Thrust (lbf)	16,966
TO TSFC (lbm/hr/lbf)	0.25

Table 5. Sample Open Rotor and GE36 Design Characteristics [9].

Parameter (units)	Sample Open Rotor	GE36 Unducted Fan
Propeller Diameter (ft)	10.9	11.7
OPR	42	27
SLS Thrust (lbf)	22,119	25,000
TSFC, M 0.8, 35,000 ft (lbm/hr/lbf)	.45	0.52

CONCLUSION AND FUTURE WORK

The renewed interest in open rotor aircraft engines due to their capacity to reduce fuel consumption has necessitated the development of open rotor cycle models. In order to develop such models within NPSS, several modeling enhancements were needed to provide analysis capabilities for counter-rotating propellers and turbines. In addition, the implementation of a multi-design point methodology and a simple power management scheme allow for rapid cycle design and exploration of the entire flight envelope.

While this work has provided a step forward in open rotor cycle analysis capabilities, there still remains room for dramatic improvement in open rotor modeling and analysis. First, the model presented here is based on a limited amount of historic, publicly available counter-rotating propeller performance data. Several engine companies are currently designing and testing new propeller designs. If these performance data are made available, the data can be converted into performance maps and used in the cycle model. Additionally, if analytical counter-rotating propeller performance codes are developed or identified, it may be possible to integrate (i.e., “wrap”) them into the NPSS framework so that new propeller designs can be evaluated. By implementing an analytical propeller performance code, a more detailed understanding of counter-rotating propeller performance and its impact on the cycle design could be achieved.

Next, further investigation regarding counter-rotating turbine performance estimation is needed. While the current model using a single turbine element will provide reasonable performance estimates for conceptual design, it does not allow for more detailed studies of open rotor design. A more complete theoretical understanding of counter-rotating turbine

performance needs to be established which will lead to a sophisticated counter-rotating turbine model within NPSS. By improving the turbine and propeller models, a better understanding will be developed regarding the interaction and coupling of these components and the limits those effects place on the design of such systems.

Finally, if improved models for the counter-rotating propellers and turbines are implemented, the power management scheme will need to be reevaluated. This will be especially necessary if the new models demonstrate a high degree of coupling between the two systems as the performance characteristics may change.

The development of the new capabilities described in this paper will make possible future open rotor cycle studies and aircraft design studies. NASA is interested in evaluating several different open rotor configurations, specifically tractor/pusher and geared/ungeared variations. Many of the developments described in this paper, including the propeller performance modeling, multi-design point sizing and power management strategy, will be applicable to the modeling of all these open rotor engine architectures. The evaluation of these open rotor configurations will also be conducted at the vehicle level so that a meaningful comparison can be carried out between open rotors, high-bypass ratio turbofans and geared turbofan engines.

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ANNEX A

COUNTER-ROTATING PROPELLER RESPONSE SURFACE EQUATIONS

Thrust coefficient for cruise Mach numbers:

$$C_T = 0.477858888468182 + 7.06020237179521 \times M + 0.106298212735099 \times \beta - 4.2264950825376 \times J \\ - 3.66227236419897 \times M^2 - 0.135610213199312 \times M \times \beta - 0.000855628477643638 \times \beta^2 \\ + 1.56685453798423 \times M \times J + 0.0712347127445022 \times \beta \times J - 0.315151540318393 \times J^2$$

Thrust coefficient for takeoff Mach numbers:

$$C_T = -2.82997954389849 + 0.180742434146289 \times \beta - 1.1579348683331 \times J + 0.0158989848771736 \times \beta \times J \\ - 0.158269167605173 \times J^2 - 0.00172659713577937 \times \beta^2$$

Power coefficient for cruise Mach numbers:

$$C_P = 19.799023228925 + 18.4702389814161 \times M - 0.590047973770211 \times \beta - 9.99634088349976 \times J \\ - 10.0200863814251 \times M^2 - 0.367383133097003 \times M \times \beta + 0.00635741314998766 \times \beta^2 \\ + 4.60880216127912 \times M \times J + 0.185060516036581 \times \beta \times J - 1.08805807929953 \times J^2$$

Power coefficient for takeoff Mach numbers:

$$C_P = -3.87744594552613 + 0.167892520010464 \times \beta - 0.0438743949610855 \times J - 0.0215083034537208 \times \beta \\ \times J - 0.237242660435654 \times J^2$$